Optimum Insulation Thickness for Walls and Roofs for Reducing Peak Cooling Loads in Residential Buildings in Lahore

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ABSTRACT

Thermal insulation is the most effective energy saving measure for cooling in buildings. Therefore, the main subject of many engineering investigations is the selection and determination of the optimum insulation thickness. In the present study, the optimum insulation thickness on external walls and roofs is determined based on the peak cooling loads for an existing residential building in Lahore, Pakistan. Autodesk® Revit 2013 is used for the analysis of the building and determination of the peak cooling loads. The analysis shows that the optimum insulation thickness to reduce peak cooling loads up to 40.1% is 1 inch for external walls and roof respectively.

Key Words: Insulation, Energy Saving, Optimum Thickness, Residential, Cooling Loads.

1. INTRODUCTION

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Lahore is the second largest city in Pakistan with latitude 31.5°N and longitude 74.3°E. The climate of Lahore is

featured as composite climate, with rainy, long and extremely hot summer; foggy winter; dry autumn and pleasant spring. The typical daytime temperature in January is about 18°C and nighttime average temperature is 6°C. While in the month of June, the average day time temperature exceeds 40°C and nighttime average temperature is 30°C. Thus due to long sunny and hot climate, the major part of electric energy is used for cooling to achieve thermal comfort [3].

In Pakistan, buildings are the major sector of energy consumption and utilize about 76% of total electricity [4]. Therefore, a lot of energy would conserve by making these building energy efficient. The use of the insulation materials in external walls and roof is the direct and effective way to decrease the heat transfer

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and electricity consumption [5]. However, it always leads to higher investment. Thus, the determination of the optimum thickness which could make the balance between the decreased energy consumption and increased investment of insulation layer is the scope of present work.

A wide range of organizations such as NREL (National Renewable Energy Laboratory) in USA, have examined the green building design and energy efficiency in buildings in different climates [6]. Bolatturk [7] studied the optimum thickness for walls with respect to cooling and heating degree hours in the warmest zone of Turkey and Yu, et. al. [8], investigated on the optimal insulation thickness for the hot summer and cold winter zone of China where as Friess, et. al. [9], measured the wall insulation for the residential villas in Dubai.

In Pakistan, only a few studies are available related to the energy conservation through thermal insulation. Ahmad, et. al. [10], studied the effect of low cost roof insulating material on indoor temperature of building in Lahore. But none specifically examine the optimal thickness of insulation for buildings in Lahore.

2. METHODOLOGY OF RESEARCH

The objective of this work is to determine the optimum insulation thickness for wall and roof of residential buildings in Lahore on the basis of percentage reduction in peak cooling loads which is the key measure to conserve electricity. Peak cooling load is the amount of heat that must be removed over an hour's time to keep the space cool on the hottest day of summer. While designing the typical building air conditioning system, it must meet the peak cooling loads of building. With the increase in insulation thickness walls and roof, peak cooling load decreases and energy conservation increases. The other parameters which influence the optimal insulation thickness and used to make the quantitative comparison among the different insulation thicknesses are U-value and investment cost. U-value is the overall heat transfer coefficient, measures the effectiveness of a material in conducting heat and decrease with the increase in insulation thickness while investment cost is become quite higher with increasing thicknesses. A single family residential building is selected as case study. A virtual model of the case study building was created in Autodesk® Revit 2013 with necessary environmental data for simulation of cooling loads and determination of U-values and investment cost.

Autodesk® Revit 2013 is the BIM (Building Information Modeling) software which allows the user to design with completely integrated database with parametric drafting and modeling element. It contains the functionality of Revit Architecture, Revit MEP and Revit Structure in a single software application [11]. The environmental data for simulation in Revit includes the building construction data, glazing data, condition type, occupancy, sensible and latent heat gain values for electric loads, set point temperature and weather data. The construction, glazing, sensible and latent heat gain data is taken from ASHARE and CBISE standards. The condition type (heating only, cooling only or both), occupancy and set point temperature is defined according to the user requirements. The climatic data of Autodesk Revit comprises of annual weather data and design dry bulb temperature of each month. The values are taken from ASHRAE 2005 database of daily range and profile of dry-bulb temperature [12].

The building model is prepared in Revit Architecture and analysis is performed by Revit MEP. MEP is an intuitive mechanical, electrical and plumbing system design tool as well as integrated with building performance analysis tools to perform heating and cooling loads analysis, day lighting analysis and more to support sustainable design. The heating and cooling loads calculation in Revit MEP follows the ASHARE standards and based on the RTS (Radiant Time Series) method. This method follows the time delay effect as heat is transmitted into spaces from exterior and from the envelopes. The overview of RTS method is shown in Fig. 1.

The important areas of RTS method are computation of conductive heat gain, the splitting of all heat gains into radiant and convection portions and the conversion of heat gains into cooling loads. The conductive heat gain is calculated for each wall and roof type from Equation (1) by using 24 response factors which gives a time series solution to the transient, one dimensional conductive heat transfer problem.

$$q_{\theta} = A \sum_{i=0}^{23} Y_{Pj} (t_{e,\theta-j\delta} - t_{rc})$$
⁽¹⁾

where q_{e} is hourly conductive heat gain, Btu/h (W), for the surface, A is surface area, ft² (m²), $Y_{p_{j}}$ is jth response factor, $t_{e,e,j\bar{a}}$ is sol-air temperature, °F(°C), j hours ago, and t_{re} is presumed constant room air temperature, °F(°C).

The next step is simplifies the conductive heat gains by splitting into radiative and convective portions. The convective portion instantly contributes to cooling load while radiative portion is absorbed by the thermal mass in the zone and then convected into the space which creates a time lag and damping effect. Therefore, the radiant portion of hourly heat gain is converted into cooling loads from Equation (2) by using radiant time factors on the basis of current and past heat gain.

$$Q_{\theta} = \sum_{n=0}^{23} r_n q_{\theta - n\delta}$$
⁽²⁾



FIG. 1. OVERVIEW OF RADIANT TIME SERIES METHOD [13]

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Where Q_{e} is Cooling load (Q) for the current hour (è), Btu/h (W), $q_{e-n\bar{a}}$ is the radiant gain at j hours ago, Btu/h (W), and r_n is the nth time radiant factor, Btu/h (W).

3.1 The Base Case Building

The case study building is located in T-Block, Phase-VIII, DHA Society, Lahore which served as base case. The selected building is recently constructed and representative of similar other residential buildings. It is a double storey single family residential building with covered area 2725 sq.ft (total area 4500 sq.ft). Its architectural planning as shown in Fig. 2(a-b), is fully compliance with the DHA bylaws. The orientation of the building is 39°N. The design conditions are considered according to ASHRAE standards and building is simulated with conventional construction materials which described in Table 1.





3.2 Modifications in Base Case

The building walls and roof for the base case were modified by applying varying thicknesses of extruded polystyrene as insulation. Extruded polystyrene (XPS Diamond Jumbolon) is closed cell, locally available best insulation to reduce the thermal conductivity. It is more acceptable insulation than the other due to its high insulation performance, long term reliability, stable R-value, moisture resistance, strength and easy installation process without any special skills[14-15]. Only need is to place polythene sheets above the foam (extruded polystyrene) to protect from fresh concrete and water [16]. Its density is 32 kg/m³ and thermal conductivity is 0.026 W/mK. Seven modifications to the walls and seven to the roof as shown in Table 2 were analyzed.



FIG. 2(b). ARCHITECTURAL PLAN (FIRST FLOOR)

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3.2.1 **Wall Modifications**

Walls are externally modified by adding the insulation with varying thicknesses ranging from 0.5, 1, 1.5, 2, 2.5, 3,4. External insulation to wall involves plastering the brick work to provide a smooth surface, attachment of the insulation boards using cement adhesive and mechanical fixings, and inclusion of a fiber mesh in the final surface plastering and additional work to deal with openings and corners is required which needs more cost than roof i.e. 100 Rs/ft² for 1 inch thickness.

3.2.2 **Roof Modifications**

The roof is modified by adding the insulation with varying thicknesses ranging from 0.5, 1, 1.5, 2, 2.5, 3,4 underneath the light weight concrete. The investment cost for roof insulation is 68 Rs/ft² for 1 inch thickness. The mud phuska is retained in roof to prompt the consideration of mixing old and new techniques of insulation instead of totally replace the older techniques which are less expensive.

Parameters and U-values	Characteristics of Model					
No of floors	2					
Floor Height	12 ft.					
Total Area	4500 sq.ft					
	0'-1/2" Ceramic Floor Tiles					
	0'-2" Concrete					
Ground Floor (U-Value= 1.330 W/m2.K)	0'-4" Brick Ballast					
	0'-4" Sand					
	0'-9" Earth					
	0'-3/8" Plaster					
Wall (U-Value= 1.880 W/m2.K)	0'-9" Brick Masonry					
	0'-3/8" Plaster					
	0'-1 1/2" Roof Tile					
	0'-2" Concrete Light Weight					
Roof (U-Value= 1.290 W/m2.K)	0'-3" Mud Phuska					
	0'-3/8" Bitumen					
	0'-6" Roof Slab Concrete (1:2:4)					
Glazing (U-Value= 5.440 W/m2.K)	0'-1/2" Glass Standard					
Model Thermal Zone	Bed Rooms, Lounge and Drawing Room on both floors					
Condition type	Cooling only					
Occupancy	8 occupants					
Air infiltration rate	0.5 ac/hr					
Sensible heat gain(per person)	110 Btu/hr					
Latent heat gain(per person)	185 Btu/hr					
Set point temperature	260C					

TABLE 1. BASE CASE BUILDING MODEL CHARACTERISTICS (AUTODESK REVIT LIBRARY DATA)

4. **RESULTS AND DISCUSSION**

The base case and all the modifications were analyzed by Autodesk® Revit and their U-value, peak cooling loads, percentage difference with respect to base case and investment cost were calculated shown in Table 2.

It is clearly visible that increasing insulation has its primary effect in the summertime, when the gains through walls and roof are the largest and that the base case has higher peak cooling loads as compare to all other insulation modifications.

The results show that the insulation modifications in roof have significantly reduced the cooling load of the building as shown in Fig 3. The roof with 1/2 inch and 1 inch insulation showing a decrease of 15.5 and 29.5% respectively in the peak cooling load compared to the

base case. The roof with 1.5, 2 and 2.5 inches thicknesses show a decrease of 31.9, 33.2 and 33.8% respectively. The roof with 3 inch is depicting a decrease of 34.1%. The roof with 4 inches thickness shows a decrease of 34.5%.



FIG. 3. COMPARISON OF PEAK COOLING LOADS BY MODIFICATIONS IN ROOF

TABLE 2.	WALL AND	ROOF	MODIFICA	TIONS,	THEIR	PEAK	COOLING	LOADS,	PERCENTAG	E DIFFERE	INCE,
				IN	VESTM	IENT C	OST				

	Modifications	U-value (W/m ² .K)	Peak Cooling Load (kW)	Difference (%)	Investment Cost (PKR)
Base Case	RW - base case	- 21.34 -		-	
Roof Modifications	R1/2W - base case+ 0.5(in) XPS in roof	0.88	18.032	15.5	93064
	R1W - base case+ 1(in) XPS in roof	0.580	15.002	29.5	147088
	R1.5W - base case+ 1.5(in) XPS in roof	0.48	14.554	31.9	201112
	R2W - base case+ 2(in) XPS in roof	0.38	14.34	33.2	255136
	R2.5W - base case+ 2.5(in) XPS in roof	0.33	14.106	33.8	309160
	R3W - base case+ 3(in) XPS in roof	0.28	14.042	34.1	363184
	R4W - base case+ 4(in) XPS in roof	0.22	13.871	34.5	471232
Wall Modifications	RW1/2 - base case+ 0.5 (in) XPS in wall	1.11	20.038	6.1	284160
	RW1 - base case+ 1(in) XPS in wall	0.670	19.163	10.2	390720
	RW1.5 - base case+ 1.5 (in) XPS in wall	0.540	18.801	11.9	497280
	RW2 - base case+ 2(in) XPS in wall	0.410	18.608	12.8	603840
	RW2.5 - base case+ 2.5 (in) XPS in wall	0.360	18.523	13.2	710400
	RW3 - base case+ 3(in) XPS in wall	0.3	18.48	13.4	816960
	RW4 - base case+ 4(in) XPS in wall	0.230	18.416	13.7	1030080

The percentage difference of the peak cooling loads of roof insulation having different thicknesses from peak cooling load of base case is shown in Fig. 4. Thus the significant percentage difference of 29.7% of roof from base case is achieved with 1 inch insulation and only a 6% difference results with increase thickness from 1 inch to 4 inch. It shows that the incremental increase in insulation thickness progressively deliver the reducing benefits because insulation is provided to cut off heat gain and up to 1 inch thick insulation maximum heat gain is block and further increase in insulation thickness has no significant effect on ceasing the heat gain but the investment cost is increased too much and energy saving increases only 6%. Thus the use of 1 inch insulation in roof is much economical.

The results show that insulation modifications in wall reduced the cooling load of the building as shown in Fig. 5. The wall with $\frac{1}{2}$ and 1 inch insulation showing a decrease of 6.1 and 10.2% respectively in the peak cooling load compared to the base case. The wall having 1.5, 2 and 2.5 inches thickness shows a decrease of 11.9, 12.8 and 13.2% respectively. The wall with 3 inches shows a decrease of 13.4% while the wall with 4 inches thickness results a decrease of 13.7%.

The percentage difference of the peak cooling loads of wall insulation having different thicknesses from peak



cooling load of base case is shown in Fig. 6. A significant percentage difference of 10.2% of wall with 1 inch insulation from base case is noted. Only a 4% of difference results with increasing the thickness from 1 to 4 inches. Using 4 inches insulation in wall will increase the cost of the building to much extent; however the use of 1 inch insulation in wall is much economical.

The Table 3 shows the simultaneously applied insulation modifications in roof and walls, their percentage difference from base case and investment cost of insulation. Since seven modifications to the walls and roof were formed and total 49 combinations for wall and roof insulation were analyzed.



FIG. 5. COMPARISON OF PEAK COOLING LOADS BY MODIFICATIONS IN WALL



FIG. 6. PERCENIAGE DIFFERENCE OF WALL INSULATION VARIATIONS FROM BASE CASE

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TABLE 3. COMBINATIONS OF WALL AND ROOF INSULATION, THEIR PEAK COOLING LOADS, PERCENTAGE DIFFERENCE AND INVESTMENT COST

Combinations of Wall and Roof Insulation	Peak Cooling Load (kW)	Difference (%)	Investment Cost (PKR)
R1/2 W1/2 - base case+0.5(in) XPS in roof+ 0.5(in) XPS in wall	16.795	21.3	377224
R1 W1/2 - base case+1(in) XPS in roof+ 0.5(in) XPS in wall	15.92	25.4	431248
R1.5 W1/2 - base case+1.5(in) XPS in roof+ 0.5(in) XPS in wall	15.514	27.3	485272
R2 W1/2 - base case+2(in) XPS in roof+ 0.5(in) XPS in wall	15.301	28.3	539296
R2.5 W1/2 - base case+2.5(in) XPS in roof+ 0.5(in) XPS in wall	15.194	28.8	593320
R3 W1/2 - base case+3(in) XPS in roof+ 0.5(in) XPS in wall	15.13	29.1	647344
R4 W1/2 - base case+4(in) XPS in roof+ 0.5(in) XPS in wall	15.066	29.4	755392
R1/2 W1 - base case+0.5(in) XPS in roof+ 1(in) XPS in wall	15.984	25.1	483784
R1W1 - base case+1(in) XPS in roof+ 1(in) XPS in wall	12.783	40.1	537808
R1.5 W1 - base case+1.5(in) XPS in roof+ 1(in) XPS in wall	12.527	41.3	591832
R2W1 - base case+2(in) XPS in roof+ 1(in) XPS in wall	12.271	42.5	645856
R2.5 W1 - base case+1.5(in) XPS in roof+ 1(in) XPS in wall	12.228	42.7	699880
R3W1 - base case+3(in) XPS in roof+ 1(in) XPS in wall	12.121	43.2	753904
R4W1 - base case+4(in) XPS in roof+ 1(in) XPS in wall	12.036	43.6	861952
R1/2 W1.5 - base case+0.5(in) XPS in roof+ 1.5 (in) XPS in wall	13.786	35.4	590344
R1 W1.5 - base case+1(in) XPS in roof+ 1.5 (in) XPS in wall	12.996	39.1	644368
R1.5 W1.5 - base case+1.5(in) XPS in roof+ 1.5 (in) XPS in wall	12.612	40.9	698392
R2 W1.5 - base case+2(in) XPS in roof+ 1.5 (in) XPS in wall	12.377	42	752416
R2.5 W1.5 - base case+2.5(in) XPS in roof+ 1.5 (in) XPS in wall	12.313	42.3	806440
R3 W1.5 - base case+3(in) XPS in roof+ 1.5 (in) XPS in wall	12.206	42.8	860464
R4 W1.5 - base case+4(in) XPS in roof+ 1.5(in) XPS in wall	12.185	42.9	968512
R1/2 W2 - base case+0.5(in) XPS in roof+ 2 (in) XPS in wall	13.039	38.9	696904
R1W2 - base case+1(in) XPS in roof+ 2(in) XPS in wall	12.335	42.2	750928
R1.5 W2 - base case+0.5(in) XPS in roof+ 2(in) XPS in wall	12.142	43.1	804952
R2W2 - base case+2(in) XPS in roof+ 2(in) XPS in wall	12.014	43.7	858976
R2.5 W2 - base case+2.5(in) XPS in roof+ 2 (in) XPS in wall	11.95	44	913000
R3W2 - base case+3(in) XPS in roof+ 2(in) XPS in wall	11.929	44.1	967024
R4W2 - base case+4(in) XPS in roof+ 2(in) XPS in wall	11.609	45.6	1075072
R1/2 W2.5 - base case+0.5(in) XPS in roof+ 2.5 (in) XPS in wall	12.697	40.5	803464
R1 W2.5 - base case+1(in) XPS in roof+ 2.5 (in) XPS in wall	11.929	44.1	857488
R1.5 W2.5 - base case+1.5(in) XPS in roof+ 2.5 (in) XPS in wall	11.545	45.9	911512
R2 W2.5 - base case+2(in) XPS in roof+ 2.5 (in) XPS in wall	11.417	46.5	965536
R2.5 W2.5 - base case+2.5(in) XPS in roof+ 2.5 (in) XPS in wall	11.332	46.9	1019560
R3 W2.5 - base case+3(in) XPS in roof+ 2.5 (in) XPS in wall	11.31	47	1073584
R4 W2.5 - base case+4(in) XPS in roof+ 2.5(in) XPS in wall	11.268	47.2	1181632
R1/2 W3 - base case+0.5(in) XPS in roof+ 3 (in) XPS in wall	12.783	40.1	910024
R1W3 - base case+1(in) XPS in roof+ 3(in) XPS in wall	12.185	42.9	964048
R1.5 W3 - base case+1.5(in) XPS in roof+ 3 (in) XPS in wall	11.929	44.1	1018072
R2W3 - base case+2(in) XPS in roof+ 3(in) XPS in wall	11.78	44.8	1072096
R2.5 W3 - base case+2.5(in) XPS in roof+ 3 (in) XPS in wall	11.694	45.2	1126120
R3W3 - base case+3(in) XPS in roof+ 3(in) XPS in wall	11.588	45.7	1180144
R4W3 - base case+4(in) XPS in roof+ 3(in) XPS in wall	11.502	46.1	1288192
R1/2 W4 - base case+0.5(in) XPS in roof+ 4 (in) XPS in wall	12.569	41.1	1123144
R1W4 - base case+1(in) XPS in roof+ 4(in) XPS in wall	12.121	43.2	1177168
R1.5 W4 - base case+1.5(in) XPS in roof+ 4 (in) XPS in wall	11.822	44.6	1231192
R2W4 - base case+2(in) XPS in roof+ 4(in) XPS in wall	11.588	45.7	1285216
R2.5 W4 - base case+2.5(in) XPS in roof+ 4 (in) XPS in wall	11.545	45.9	1339240
R3W4 - base case+3(in) XPS in roof+ 4(in) XPS in wall	11.438	46.4	1393264
R4W4 - base case+4(in) XPS in roof+ 4(in) XPS in wall	11.289	47.1	1501312

It is clear that 4 inches insulation thickness in roof and 4 inches insulation thickness in wall (R4W4) shows the least peak cooling load. Only 1 inch insulation thickness in roof and 1 inch insulation thickness in wall advocates a significant peak cooling load difference from base case. The difference among the peak cooling loads of all other combinations with increase in insulation seems non-significant as shown in Fig. 7. It is inferred that for economical solution modification with 1 inch insulation thickness in wall (R1W1) should be used.

5. CONCLUSIONS

The present study has analyzed the thermal performance of a single-family double storey residential building in Lahore to determine the optimum insulation thickness for building roof and walls based on peak cooling loads. The envelope with 4 inches insulation thickness in roof and 4 inches thickness in walls shows the least peak cooling loads reduction of 47.1% from base case. The construction cost increases with the thickness of insulation and hence, increases the overall cost of the building.

For the cost effective construction, the external wall having 1 inch external layer of extruded polystyrene and

the 1 inch insulation layer in roof is considered as optimum insulation thickness for energy efficient and cost effective construction, which show nearly the same results i.e. peak cooling loads reduction of 40.1%, but its construction is cheaper. So this modification can be considered for cost effectiveness.

For cost effective energy efficient envelope construction, it is concluded that the effect of insulation on roof is much significant as compared with the effect of insulation on walls. Therefore in some cases to make cost effective construction the insulation can be applied to roof only which would also give a significant decrease in peak cooling loads.

6. FUTURE WORK

The whole building life cost and projected energy cost savings data will be incorporated in future study to enhance the assessment of optimum insulation and calculation of payback period.

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FIG. 7. COMPARISON OF PEAK COOLING LOADS BY MODIFICATIONS IN BOTH WALL AND ROOF

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